

International Monetary Economics

Georg Stadtmann
stadtmann@europa-uni.de

Chapter 15 Money, Interest Rates, and Exchange Rates

How to set up a model

- 1 Define the equilibrium conditions
- 2 Derive the slope of the curves
- 3 Determine equilibrium
- 4 Identify the shock: It is always an *exogenous* variable, which changes in the beginning!
- 5 Which curve shifts in which direction? Use the equations!
- 6 Shift the curves and determine new equilibrium.
- 7 Confirm graphical results by computing the multipliers.
- 8 Compare and conclude.

Equations of the monetary model

$$(1) \quad \bar{y} = \delta(e + p^* - p) + \gamma\bar{y} + g$$

Goods market equilibrium condition

$$(2) \quad m - p = \phi\bar{y} - \lambda R$$

Money market equilibrium condition

$$(3) \quad R = R^*$$

UIP-Condition

Greek letters: positive parameters

All variables except interest rates are in logs.

Why in logs?

$$(4) \quad \frac{M}{P}$$

Suppose, we want to derive the total differential:

$$(5) \quad \frac{M}{P} = M \cdot P^{-1}$$

$$(6) \quad P^{-1}dM + (-1) \cdot MP^{-1-1} \cdot dP = \frac{dM}{P} - \frac{M}{P^2} \cdot dP$$

Writing equation (4) in natural logs: $m - p$. Total differential:

$$(7) \quad dm - dp$$

Goods market equilibrium condition

$$\bar{y} = \delta(e + p^* - p) + \gamma\bar{y} + g$$

- $(e + p^* - p)$ natural log of the real exchange rate.
- No investment \Rightarrow goods demand does not depend in a negative way on the domestic interest rate.

Greek letters

- δ : delta
- γ : gamma
- ϕ : phi
- λ : lambda

Denotation of the symbols

Endogenous variables:

- p = domestic price level
- e = nominal exchange rate (in a **floating** exchange rate system)
- R = domestic interest rate

Exogenous variables:

- p^* = foreign price level
- m = nominal money supply
- \bar{y} = domestic output level
- R^* = foreign interest rate
- g = government spending

Important: Domestic output is exogenous \Rightarrow output is capacity constrained!

Goods market equilibrium: Derivation of the IS-curve

$$(8) \quad \bar{y} = \delta(e + p^* - p) + \gamma\bar{y} + g$$

We want to solve equation for the goods price level (p):

$$(9) \quad \delta(e + p^* - p) = \bar{y} - \gamma\bar{y} - g$$

Dividing by δ leads to:

$$(10) \quad e + p^* - p = \frac{(1 - \gamma)\bar{y}}{\delta} - \frac{g}{\delta}$$

Isolating p leads to:

$$(11) \quad p = e + p^* - \frac{(1 - \gamma)\bar{y}}{\delta} + \frac{g}{\delta}$$

Goods market equilibrium: Derivation of the IS-curve

$$(12) \quad p = e + p^* - \frac{(1 - \gamma)\bar{y}}{\delta} + \frac{g}{\delta}$$

Taking the total differential leads to:

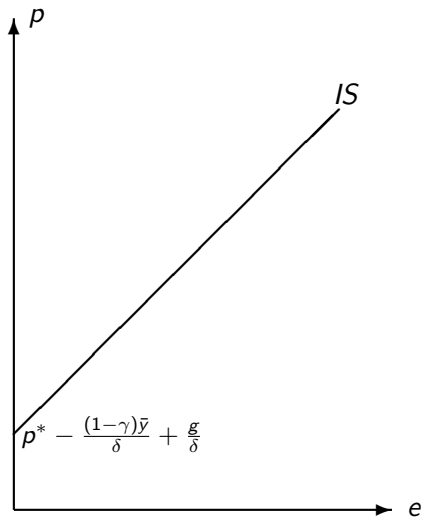
$$(13) \quad dp = de + dp^* - \frac{(1 - \gamma)d\bar{y}}{\delta} + \frac{dg}{\delta}$$

We are interested in the ratio dp/de . All other variables are held constant so that their changes are equal to zero:

$$(14) \quad dp = de \quad \Rightarrow \quad \frac{dp}{de} = 1 > 0$$

The IS-curve has a positive slope of one!

The IS-curve



Shifts of the IS-curve

$$(12) \quad p = e + p^* - \frac{(1 - \gamma)\bar{y}}{\delta} + \frac{g}{\delta}$$

- If the foreign price level increases ($p^* \uparrow$), or
- if government spending increases ($g \uparrow$), or
- if the output level decreases ($\bar{y} \downarrow$),

the IS-curve will shift upwards.

- The IS-curve does **not** shift, if the domestic price level (p) or the nominal foreign exchange rate (e) change, because these variables are displayed on the vertical/horizontal axis!

Money market equilibrium: Derivation of the LM-curve

$$(2) \quad m - p = \phi \bar{y} - \lambda R \quad (3) \quad R = R^*$$

Plugging (3) in (2) yields:

$$(15) \quad m - p = \phi \bar{y} - \lambda R^*$$

Solving for p leads to:

$$(16) \quad p = m - \phi \bar{y} + \lambda R^*$$

Money market equilibrium: Derivation of the LM-curve

$$(16) \quad p = m - \phi \bar{y} + \lambda R^*$$

Taking the total differential leads to:

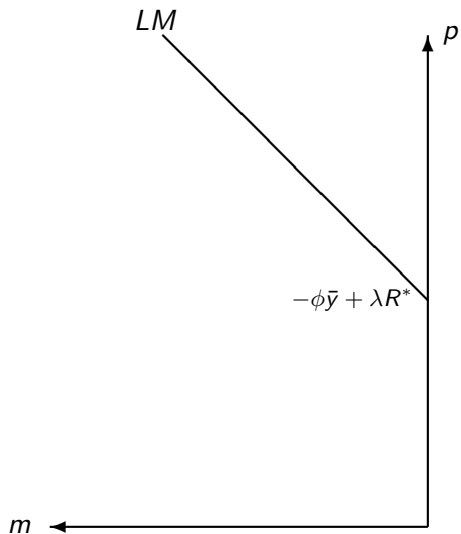
$$(17) \quad dp = dm - \phi d\bar{y} + \lambda dR^*$$

We are interested in the ratio dp/dm . All other variables are held constant so that their changes are equal to zero:

$$(18) \quad dp = dm \quad \Rightarrow \quad \frac{dp}{dm} = 1 > 0$$

The LM-curve has a positive slope of one!

LM-curve



Shifts of the LM-curve

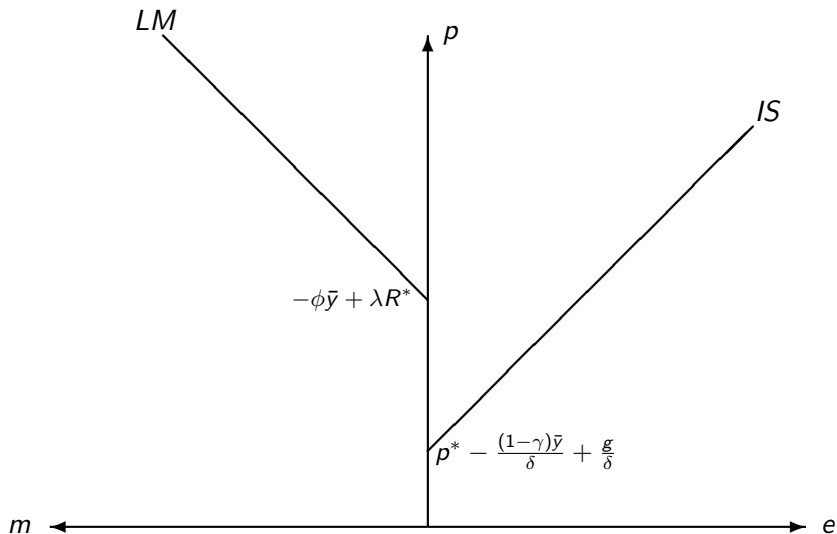
$$(16) \quad p = m - \phi \bar{y} + \lambda R^*$$

- If the foreign interest rate increases ($R^* \uparrow$) or
- if the output level decreases ($\bar{y} \downarrow$),

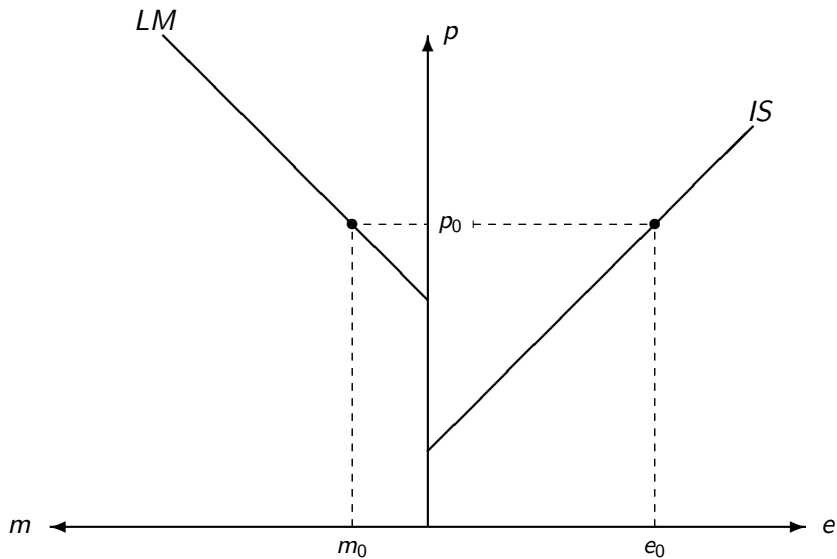
the LM-curve will shift upwards.

- The LM-curve does **not** shift, if nominal money supply (m) or the domestic price level (p) change, because these variables are displayed on the vertical/horizontal axis!

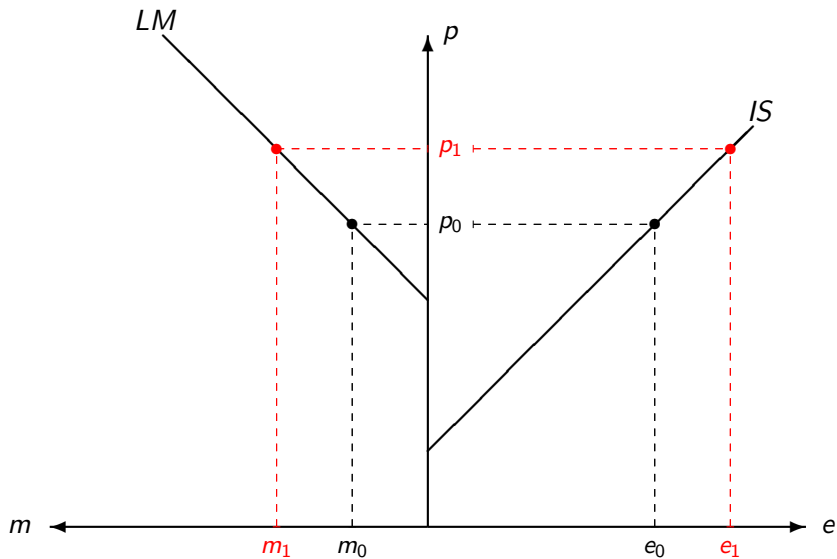
LM- and IS-curve



Equilibrium in the initial situation



Expansionary monetary policy ($m \uparrow$)



Matrix notation

$$p = e + p^* - \frac{(1-\gamma)\bar{y}}{\delta} + \frac{g}{\delta}$$

$$p = m - \phi\bar{y} + \lambda R^*$$

Writing these expressions a little bit different leads to:

$$1 \cdot p - 1 \cdot e = p^* - \frac{(1-\gamma)\bar{y}}{\delta} + \frac{g}{\delta}$$

$$1 \cdot p + 0 \cdot e = m - \phi\bar{y} + \lambda R^*$$

$$(19) \quad \begin{bmatrix} 1 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} p \\ e \end{bmatrix} = \begin{bmatrix} p^* - \frac{(1-\gamma)\bar{y}}{\delta} + \frac{g}{\delta} \\ m - \phi\bar{y} + \lambda R^* \end{bmatrix}$$

Taking the total differential yields:

$$(20) \quad \begin{bmatrix} 1 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} dp \\ de \end{bmatrix} = \begin{bmatrix} dp^* - \frac{(1-\gamma)d\bar{y}}{\delta} + \frac{dg}{\delta} \\ dm - \phi d\bar{y} + \lambda dR^* \end{bmatrix}$$

Matrix notation

$$\begin{bmatrix} 1 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} dp \\ de \end{bmatrix} = \begin{bmatrix} dp^* - \frac{(1-\gamma)d\bar{y}}{\delta} + \frac{dg}{\delta} \\ dm - \phi d\bar{y} + \lambda dR^* \end{bmatrix}$$

- We are interested in the effects of an expansionary monetary policy ($dm > 0$).
- All other variables are kept constant so that their changes are equal to zero!

$$\begin{bmatrix} 1 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} dp \\ de \end{bmatrix} = \begin{bmatrix} 0 \\ dm \end{bmatrix}$$

Price multiplier of an expansionary monetary policy

$$\begin{bmatrix} 1 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} dp \\ de \end{bmatrix} = \begin{bmatrix} 0 \\ dm \end{bmatrix}$$

Applying Cramer's rule leads to:

$$dp = \frac{\begin{vmatrix} 0 & -1 \\ dm & 0 \end{vmatrix}}{\begin{vmatrix} 1 & -1 \\ 1 & 0 \end{vmatrix}} = \frac{[0 \cdot 0] - [dm \cdot (-1)]}{[1 \cdot 0] - [1 \cdot (-1)]} = \frac{dm}{1}$$

Hence, we get for the price multiplier:

$$(21) \quad \frac{dp}{dm} = 1$$

Exchange rate multiplier of an expansionary monetary policy

$$\begin{bmatrix} 1 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} dp \\ de \end{bmatrix} = \begin{bmatrix} 0 \\ dm \end{bmatrix}$$

Applying Cramer's rule leads to:

$$de = \frac{\begin{vmatrix} 1 & 0 \\ 1 & dm \end{vmatrix}}{\begin{vmatrix} 1 & -1 \\ 1 & 0 \end{vmatrix}} = \frac{[1 \cdot dm] - [1 \cdot 0]}{[1 \cdot 0] - [1 \cdot (-1)]} = \frac{dm}{1}$$

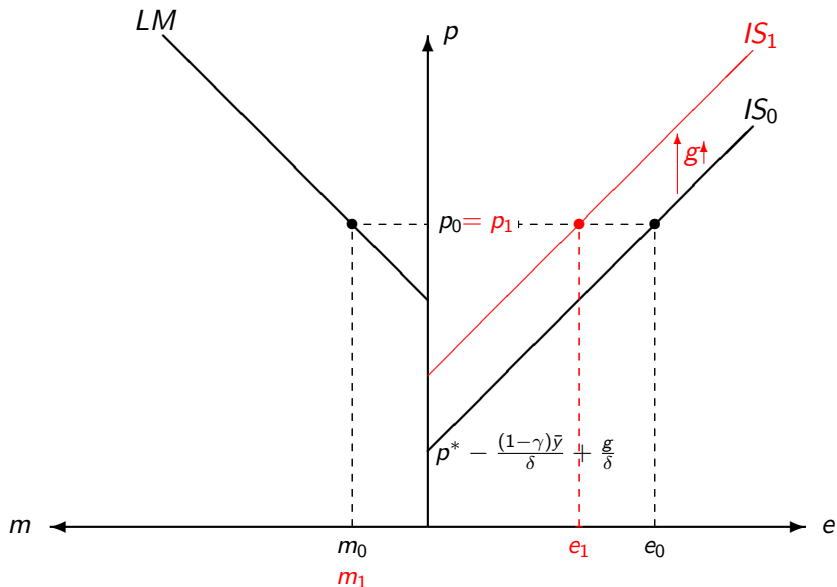
Hence, we get for the exchange rate multiplier:

$$(22) \quad \frac{de}{dm} = 1$$

Conclusion: Monetary policy

- An increase in the nominal money supply leads to an increase in prices and the nominal exchange rate on a 1:1 basis.
- The real exchange rate is constant.
- Classical dichotomy: Money is neutral.
- Monetary variables do not influence real variables.

Expansionary fiscal policy



Price multiplier of an expansionary fiscal policy

$$\begin{bmatrix} 1 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} dp \\ de \end{bmatrix} = \begin{bmatrix} \frac{dg}{\delta} \\ 0 \end{bmatrix}$$

Applying Cramer's rule yields:

$$dp = \frac{\begin{vmatrix} \frac{1}{\delta} dg & -1 \\ 0 & 0 \end{vmatrix}}{\begin{vmatrix} 1 & -1 \\ 1 & 0 \end{vmatrix}} = \frac{[\frac{1}{\delta} dg \cdot 0] - [0 \cdot (-1)]}{[1 \cdot 0] - [1 \cdot (-1)]}$$

$$(23) \quad \frac{dp}{dg} = 0$$

Exchange rate multiplier of an expansionary fiscal policy

$$\begin{bmatrix} 1 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} dp \\ de \end{bmatrix} = \begin{bmatrix} \frac{dg}{\delta} \\ 0 \end{bmatrix}$$

Applying once more Cramer's rule:

$$de = \frac{\begin{vmatrix} 1 & \frac{1}{\delta} dg \\ 1 & 0 \end{vmatrix}}{\begin{vmatrix} 1 & -1 \\ 1 & 0 \end{vmatrix}} = \frac{[1 \cdot 0] - [1 \cdot \frac{1}{\delta} dg]}{[1 \cdot 0] - [1 \cdot (-1)]} = \frac{-\frac{1}{\delta} dg}{1}$$

$$(24) \quad \frac{de}{dg} = -\frac{1}{\delta} < 0$$

Conclusion: Expansionary fiscal policy

- A fiscal expansion does not influence the domestic price level.
- Fiscal expansion decreases nominal exchange rate.
- Domestic currency appreciates in nominal terms ($e \downarrow$).
- Since prices are constant: Nominal appreciation leads to a real appreciation.
- Real exchange rate changes.
- Real appreciation crowds out foreign demand for domestic goods.
- Complete exchange rate induced crowding out effect!

Frequent mistakes

- When it comes to Cramer's Rule: Students use brackets instead of determinant signs ('straight lines')